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Fitting statistical distributions to sea duck count data: Implications for survey design and abundance estimation

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ABSTRACT

Determining appropriate statistical distributions for modeling animal count data is important for accurate estimation of abundance, distribution, and trends. In the case of sea ducks along the U.S. Atlantic coast, managers want to estimate local and regional abundance to detect and track population declines, to define areas of high and low use, and to predict the impact of future habitat change on populations. In this paper, we used a modified marked point process to model survey data that recorded flock sizes of Common eiders, Long-tailed ducks, and Black, Surf, and White-winged scoters. The data come from an experimental aerial survey, conducted by the United States Fish & Wildlife Service (USFWS) Division of Migratory Bird Management, during which east-west transects were flown along the Atlantic Coast from Maine to Florida during the winters of 2009–2011. To model the number of flocks per transect (the points), we compared the fit of four statistical distributions (zero-inflated Poisson, zero-inflated geometric, zero-inflated negative binomial and negative binomial) to data on the number of species-specific sea duck flocks that were recorded for each transect flown. To model the flock sizes (the marks), we compared the fit of flock size data for each species to seven statistical distributions: positive Poisson, positive negative binomial, positive geometric, logarithmic, discretized lognormal, zeta and Yule–Simon. Akaike's Information Criterion and Vuong's

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closeness tests indicated that the negative binomial and discretized lognormal were the best distributions for all species for the points and marks, respectively. These findings have important implications for estimating sea duck abundances as the discretized lognormal is a more skewed distribution than the Poisson and negative binomial, which are frequently used to model avian counts; the lognormal is also less heavy-tailed than the power law distributions (e.g., zeta and Yule–Simon), which are becoming increasingly popular for group size modeling. Choosing appropriate statistical distributions for modeling flock size data is fundamental to accurately estimating population summaries, determining required survey effort, and assessing and propagating uncertainty through decision-making processes.

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1. Introduction

Effective management of wildlife populations requires high quality estimates of population abundance and distribution with associated measures of uncertainty. Managers use abundance estimates to determine population status, for comparison to environmental carrying capacities, and to monitor population trends [44]. Understanding patterns of abundance and aggregation is necessary at both regional and local scales to evaluate the impacts of conservation actions and human disturbance. Obtaining accurate population indices is difficult, however, because animals are often unevenly and unpredictably distributed [8,9,43]; for example, counts often include many zeros [19,30] and distributions of count data can be extremely right skewed [4,17]. The problem is compounded by a need for consistent repeated estimates over time; yet, sufficient data to characterize highly aggregated species distributions are expensive to collect and maintain. The choice of appropriate statistical models for wildlife count distributions is fundamental for consistency and efficiency of abundance and distribution estimation and to facilitate more reliable uncertainty assessments [48].

Waterfowl managers are especially interested in population estimates for five species of North American sea ducks (Tribe Mergini) that winter in large numbers off the Atlantic coast of the United States (Sea Duck Joint Venture 2003). Data from a variety of sources suggest that Common eiders (*Somateria mollissima*), Long-tailed ducks (*Clangula hyemalis*), and Black, Surf, and White-winged scoters (*Melanitta nigra*, *M. perspicillata*, and *M. fusca*) may be declining [36,42], and proposed offshore energy development has the potential to significantly alter their wintering habitat [13,15,25]. Waterfowl managers need accurate and precise coast-wide winter abundance indices to assess trends and set annual harvest regulations, while energy regulators need predictions of spatial variation in abundance to inform responsible site placement of offshore structures and to guide future development activities.

During the winter, sea ducks form large foraging flocks, but can also be found alone or in small groups [7]. Their distributions can shift within and between years, due to changes in habitat, weather, and prey availability [18,24,26,52], and they can be found up to 40 miles from land [41]. As a result, effective monitoring surveys are expensive, dangerous, and fraught with logistical challenges. If the resulting data are to be worth collecting, then appropriate statistical models to interpret the data need to be available and accessible.

The United States Fish and Wildlife Service (USFWS) Division of Migratory Bird Management initiated an experimental aerial survey, conducted from Maine to Florida in the winters of 2009–11, to assess the feasibility and effectiveness of a long-term winter sea duck monitoring program along the Atlantic coast. Determining whether precise estimates of regional annual abundance are possible for the five target species is necessary to evaluate the effectiveness of the survey. To meet these objectives, we explore the fit of a set of statistical models to data from the Atlantic coast wintering sea duck survey. Our goals are: (1) to identify a model, or models, that accurately describes the distribution of counts, characterized by an unusually heavy right tail and an excessive number of zeros; (2) to determine if the best model choice varies by species; and (3) to compare parameter estimates among species and assess whether more refined models (e.g., that stratify regions by high and low density

or include habitat covariates) and/or data collection efforts are necessary. Identifying a parsimonious model is of primary importance because monitoring programs require repeated, timely estimates that are easy to explain and robust to unexpected data reduction or other survey changes. Thus, analytically complex and data-hungry approaches are ill-advised for management-oriented monitoring programs.

The most challenging problem we face is characterizing a count distribution with an extreme variance to mean ratio, as is often observed in sea duck data [52]. Identifying appropriate statistical distributions for analyzing count data of animal populations is an ongoing area of investigation in ecology. For reasons based on first principles and for convenience, the Poisson distribution has frequently been used [8] and is popular in modeling avian species (e.g., [14,28]). Yet the assumption that the variance equals the mean often does not hold for many seabird species, which are known to form large flocks. The negative binomial distribution, which allows the variance to exceed the mean, is used as an alternative to the Poisson to characterize the count distributions for species where spatial aggregation is known to occur (e.g., [2,11,49]). The negative binomial distribution is the result of a Poisson–Gamma mixture and converges to the Poisson distribution as the shape parameter, k , approaches infinity (Appendix A). Okubo [34] recommended the geometric distribution – a discrete analog to the exponential distribution and also a special case of the negative binomial where the shape parameter equals one – to handle extremely large group sizes and demonstrated its applicability for a number of taxa including birds. Empirical evidence suggests, however, that the negative binomial and geometric models do not adequately capture observed distributions of counts for some populations, especially those that are found in very large group sizes, such as some fish and bird species. Ma et al. [29] derived a logarithmic distribution from first principles based on rules for when individuals should join and leave groups; this model has outperformed the Poisson and negative binomial distributions in studies of house sparrows [17] and seabirds [21]. Ma et al. [29] additionally pointed out that the logarithmic can be derived as a limiting case of the negative binomial distribution as the shape parameter (k , Appendix A) approaches zero (see also [39]), placing it in the context of other distributions used to model ecological count data.

More recently, the power law distribution has been proposed for modeling group sizes when the variance to mean ratio is much larger than can be accommodated by the aforementioned models [3,4]. Several studies have demonstrated that the power law distribution fits well to a number of empirical examples including populations of fish, seabirds, and mammals [10,2,22,23,45]. However, the power law distribution (using ecologically relevant parameter ranges) is capable of producing extremely large counts (e.g., in the millions; [10]), which are not realistic for most sea duck species. The power law can be truncated or combined with an exponentially decaying function [33] to address this problem. In fact, Ma et al. [29] pointed out that the logarithmic distribution itself is a discrete form of a power law distribution with an exponential cutoff, where the power law exponent is -1 and the upper tail decays exponentially above a cutoff that is directly related to the average group size experienced by an individual. Bonabeau et al. [4] also presents mechanistic models of group size that lead to power law distributions with exponential decay.

Other heavy-tailed distributions exist and should be considered in a model selection context before concluding that “power law-like” behavior observed in empirical data necessarily indicates a power law distribution [10]. These include the Yule–Simon and the discretized lognormal distributions, which themselves can be viewed, respectively, as limiting distributions of stochastic preferential attachment or multiplicative growth processes [10,31]. Given the diversity of possibilities, a model selection framework would be useful to guide choices of appropriate distributions to model highly skewed ecological count data [2].

In this paper, we test the fit of a series of over-dispersed statistical distributions, from the negative binomial to the power law, to counts of sea duck flock sizes; we also assess the fit of a series of over-dispersed models to the distribution of flock frequencies. Our assessment is a critical first step in the applied statistical work needed for the development of rigorous survey designs, power analysis, risk and impact assessments, and optimal management strategies for sea ducks. Appropriate modeling of the basic underlying distributional characteristics of avian count data is critical for making strong inferences about the distribution of target populations, particularly in the marine environment where logistics are inherently more difficult than in terrestrial systems and reliance upon statistical models is correspondingly greater.

2. Methods

2.1. Data collection

The USFWS aerial survey was conducted along the Atlantic coast from the US-Canadian border ($44^{\circ} 46'N$) to Jacksonville, FL ($30^{\circ}21'N$) between January and March, 2009–2011. Four fixed-wing aircraft were flown along east–west transects spaced systematically at intervals of five minutes of latitude (approximately 5 nm apart). These transects extended east from the coastline to the longer of two distances: 8 nm or the distance to 16 m depth. Transects ranged in length from 1 to 80 nm (with 95% of transects between 4.8 and 46.4 nm). The mean transect length was 17.9 nm (standard deviation: 12.8 nm) with transects less than 8 nm in areas that span bays and longer transects paralleling the shoreline in complicated coastal areas (e.g., Long Island Sound).

The survey crews, which consisted of an observer and pilot-observer, flew at 110 knots and 70 m altitude, while counting sea ducks and other aquatic birds within 400 m-width strip transects (the observer counts a 200 m strip on one side of the plane while the pilot does the same on the opposite side). After completing their entire set of transect lines, each crew flew north to their first east–west transect line and replicated every other transect from north to south. The replicate surveys were conducted approximately one week after the first surveys and do not duplicate the original track exactly, making the possibility of recounting the same individuals remote. The three scoter species are difficult to distinguish reliably in the field, leading to a large number of scoters identified only to genus (*Melanitta* spp.). As such, we focused our analyses on generic scoter species (records for all three species combined with unidentified scoters), along with the Common eider and Long-tailed duck. We refer to these two species and one genus as the “species groups” of interest.

Surveys were conducted from 1 to 18 February in 2009, 23 January to 2 March in 2010, and 31 January to 17 February in 2011. Due to the vagaries of field operations, transects and replicates varied somewhat between years. We use data from the 236 transects, and 76 replicates that were successfully surveyed in all three years. Common eider and Long-tailed ducks do not winter in the southern portions of the survey area, and so models fit for them are based on fewer transects (88 for Common eiders, of which 21 were replicated; 173 for Long-tailed ducks, of which 54 were replicated).

The data consist of observations along survey transects recording the (1) location, (2) species, and (3) number of birds seen at the location. We refer to the group of birds recorded at one location (including single birds) as a “flock”, and the number of birds seen as the “flock size”. Note that birds are counted only within the transect boundaries, while the actual flock might have extended well beyond.

2.2. Analysis

To estimate the abundance of sea ducks by species, we represent the data as a modified marked point process [12,20] where the flocks are the points and the size of the flocks, discrete and independent of the points, are the marks. The point process is summarized by transect: we first model the flock counts (i.e., number of flocks) on each transect, and then model the flock sizes, conditional on the number of flocks observed. Preliminary analyses indicated large variations and only small correlations in the number of species-specific flocks (points) among neighboring transects (0.23 for Common eiders, 0.41 for Long-tailed ducks, and 0.24 for scoters), due in part to zero-zero neighbors in areas of low density. This suggests that the number of flocks on one transect is not predictive of the flock count on neighboring transects. We additionally found no significant relationships between the number/density of flocks per transect and the sizes of those flocks, which fits our assumption of independence in marks and points.

To determine the appropriate model to describe the observed number of flocks per transect (the point process), we tested the fit of four distributions to the transect-level flock counts: zero-inflated Poisson, zero-inflated geometric, and zero-inflated negative binomial, as well as the standard negative binomial (Appendix A). The data were fit separately for Common eiders, Long-tailed ducks, and scoter species and we included an offset for transect area (to account for variable transect lengths), which was standardized by dividing the area of each transect by the mean of all transect areas. We fit each

model using maximum likelihood estimation (MLE) in the program R (version 2.13.2; R development Core [40]) with the VGAM package [50].

For the flock size data (the marks), we fit seven discrete distributions with positive integer support (because there are no flocks of size zero): positive Poisson, positive negative binomial, positive geometric, logarithmic, discretized lognormal (a discretized version of the continuous lognormal, truncated to a minimum of one), zeta (discrete power law), and Yule–Simon (which we refer to as the Yule) distributions (Appendix B). We modeled the data for species groups separately using each statistical distribution [40]. We again estimated the parameters for distributions using MLE in the program R (version 2.13.2; [40]). We used the VGAM package [50] to estimate parameters for the positive Poisson, positive negative binomial, positive geometric, and logarithmic distributions. We used the methods and code provided in Clauset et al. [10] to estimate the parameters for the discretized lognormal, the zeta, and the Yule distributions. In applying the zeta distribution, both a shape parameter as well as a threshold (sometimes referred to as x_{\min}) can be estimated, below which data are excluded from the analysis. This is sometimes done because it is hypothesized that power law distributions may occur only above some minimum value for a given data set [10]. Because we were interested in fitting each of these distributions to the complete dataset, we set the threshold equal to one for the zeta distribution (and other distributions, where applicable).

For both the points and marks, we calculated the log-likelihood of each model. We used the likelihoods to calculate Akaike's Information Criterion corrected for finite sample sizes (AICc), which we then used to rank the models [6]. We further assessed model fit using the Vuong closeness test [47] for pair-wise comparisons of the best fitting models to the flock size data (marks). The Vuong is a likelihood-ratio test that measures whether one model is closer than the other to the unknown true model using the Kullback–Leibler information criterion [47] and can be derived for both nested and non-nested models. The benefit of using the Vuong test is that it allowed us to evaluate the hypothesis that models ranked higher based on AICc were significantly closer to the true data-generating model than lower-ranked models through estimation of a p -value. We implemented the Vuong test by generalizing the “vuong” function for non-nested models (because all top models turned out to be non-nested) in the `pscl` package in program R [51]. We then compared parameter estimates for the top models for each species group.

3. Results

There were 1742, 2709, and 4047 flocks observed from 2009 to 2011 for Common eiders, Long-tailed ducks, and scoters, respectively, with the total number of individuals being 28,968 Common eiders, 30,677 Long-tailed ducks, and 55,859 scoters. The number of flocks per transect ranged from 0 to 95 for Common eiders, 0–130 for Long-tailed ducks, and 0–104 for scoters. Even after accounting for species ranges, there were a large number of transects in which no flocks were observed: 166 out of 327 for Common eiders, 413 out of 681 for Long-tailed ducks, 525 out of 936 for scoters.

Flock size ranged from 1 to 2000 for Common eiders, 1–750 for Long-tailed ducks, and 1–5000 for scoters with the median flock size equal to three for Common eiders and Long-tailed ducks and four for scoters. However, the standard deviation of flock size was quite high: 94 for Common eiders, 39 for Long-tailed ducks, and 112 for scoters. These statistics and plots of log-frequency versus log-abundance (Fig. 1) demonstrate the right skew of the flock size distributions.

3.1. Distribution of number of flocks per transect

The negative binomial distributions (zero-inflated and standard) were the best fitting distributions for the data on the number of flocks per transect for all species groups (Table 1; this was also true for the three scoter species identified to species—results not shown). For the Common eider, the zero-inflated negative binomial distribution had a slightly higher log-likelihood (and hence lower AICc value) than the standard negative binomial. In the case of the Long-tailed ducks and scoters, the zero inflation parameter was estimated to be zero, collapsing to the standard negative binomial distribution. The zero-inflated geometric and Poisson distributions had considerably lower log-likelihoods and comparably poorer fits to the data (Table 1).

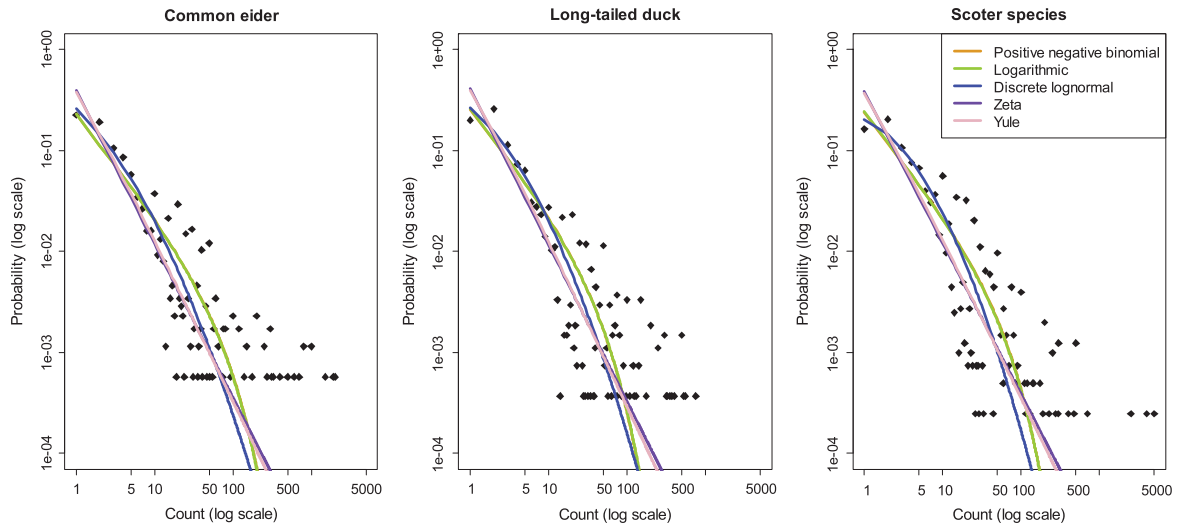


Fig. 1. Model fits (lines) and observed probabilities (black dots) for count data (marks) for the three species groups: Common eiders, Long-tailed ducks, and scoters. Fits are shown for the top 5 models: logarithmic, discretized lognormal, zeta, Yule, and positive negative binomial. The positive negative binomial fit is not visible because it is obscured by the logarithmic fit.

Table 1

Log-likelihood and parameter estimates for distributions fit to data on the number of flocks per transect for Common eiders, Long-tailed ducks, and all scoters combined. Likelihoods are presented because likelihood rankings were identical to AICc rankings (sample sizes were relatively large and the number of parameters for all fitted models ranged from 2 to 3). Specifications for each distribution are given in Appendix A. The parameter φ is the zero inflation parameter (ranging from 0 to 1) and is the probability of a structural zero. The second to last column shows the observed (sample) mean number of flocks per transect for each species (bold) and estimates of the mean under each distributional assumption. Note that the MLE of the negative binomial distribution is the sample mean by definition. The last column shows the observed proportion of transects without flocks (bold) and the proportion estimated under each distributional assumption. The zero inflated negative binomial is excluded from this table for the Long-tailed ducks and scoter species because the zero-inflated parameter was estimated to be zero, collapsing the distribution to a standard negative binomial.

	Log-likelihood	φ	Parameter estimates		Mean flocks per transect	Transects with no flocks
Common eiders						
Zero inflated negative binomial	-727.72	0.19	$\mu = 7.20$	$k = 0.43$	5.33	0.51
Negative binomial	-743.24		$\mu = 5.33$	$k = 0.24$	5.33	0.48
Zero inflated geometric	-885.62	0.07	$p = 0.55$		1.12	0.57
Zero inflated Poisson	-1444.37	0.56	$\lambda = 9.57$		4.18	0.49
Long-tailed ducks						
Negative binomial	-1162.43		$\mu = 3.98$	$k = 0.21$	3.98	0.61
Zero inflated geometric	-1644.99	0.05	$p = 0.66$		1.86	0.68
Zero inflated Poisson	-2270.05	0.45	$\lambda = 6.82$		3.73	0.45
Scoters						
Negative binomial	-1782.63		$\mu = 4.32$	$k = 0.20$	4.32	0.56
Zero inflated geometric	-2286.72	0.07	$p = 0.59$		1.33	0.61
Zero inflated Poisson	-4280.94	0.49	$\lambda = 7.80$		4.00	0.49

3.2. Distribution of flock sizes

The discretized lognormal distribution produced the best fit to the data for flock sizes of all three species groups (Table 2; Fig. 1). This was a consistent result applying to all species together (Fig. 2), each species separately (including the three scoter species when identified to species; results not shown) and each species separately by year (2009–2011; results not shown). In all cases, the discretized lognormal had the lowest AICc value when compared to the other six candidate distributions and had a significantly better fit compared to the other top models as inferred from Vuong pair-wise closeness tests (Table 2). The next best models varied by species group with the logarithmic, Yule, zeta, and positive negative binomial distributions all producing reasonable (although inferior) fits to

Table 2

Model selection results for each model fit to non-zero flock size data for Common eiders, Long-tailed ducks, all scoter species combined. Log-likelihood values are shown in the diagonals. Likelihoods are presented because likelihood rankings were identical to AICc rankings (sample sizes were relatively large and the number of parameters ranged from 1 to 2 for all fitted models). The off-diagonals report the *p*-values from pair-wise Vuong closeness tests. In all pair-wise comparisons, the distribution with the lower log-likelihood value was also identified as the best (closest to unknown true model) by the Vuong test statistic. However, the values in grey show when the difference was not significant. The positive Poisson and geometric models are excluded from our comparison because their likelihoods indicated very poor fits to our data (Common eiders: −6585.6 geom, −61,046.0 pois; Long-tailed ducks: −9160.3 geom, −48,029.6 pois; scoters: −14,519.5 geom, −111,268.9 pois).

Common eiders					
	Discretized lognormal	Yule	Zeta	Logarithmic	Positive negative binomial
Discretized lognormal	−5227.0				
Yule	<0.001	−5347.9			
Zeta	<0.001	<0.001	−5404.8		
Logarithmic	<0.001	0.049	0.333	−5425.5	
Positive negative binomial	<0.001	0.041	0.304	<0.001	−5429.3
Long-tailed ducks					
	Discretized lognormal	Yule	Logarithmic	Positive negative binomial	Zeta
Discretized lognormal	−7718.0				
Yule	<0.001	−7922.1			
Logarithmic	<0.001	0.394	−7931.6		
Positive negative binomial	<0.001	0.352	<0.001	−7935.9	
Zeta	<0.001	<0.001	0.007	0.007	−8022.5
Scoters					
	Discretized lognormal	Logarithmic	Positive negative binomial	Yule	Zeta
Discretized lognormal	−12312.9				
Logarithmic	<0.001	−12764.7			
Positive negative binomial	<0.001	<0.001	−12774.4		
Yule	<0.001	0.126	0.149	−12901.7	
Zeta	<0.001	0.005	0.008	<0.001	−13069.6

the data (Table 2; Fig. 1). For all three species, the positive negative binomial had a very similar, although slightly inferior fit as compared to the logarithmic distribution using AICc and Vuong tests (e.g., the positive negative binomial model is obscured by the logarithmic in Fig. 1). This is consistent with the fact that the logarithmic distribution is a limiting case of the negative binomial [39,29] and that the shape parameter in the negative binomial for all species was close to zero (Table 3). This was also true for the Yule and zeta distributions, whose fits were qualitatively very similar, although the Yule outperformed the zeta for all species by AICc and Vuong tests (Table 2). The geometric and positive Poisson models were the worst fitting models in all cases with likelihoods much lower than the other models (see caption for Table 2) and were thus excluded from further consideration.

In all comparisons, the direction of the Vuong test statistic supported the ranking of model fits by their AICc values (and by their log-likelihoods). The discretized lognormal had a significantly better fit as compared to the other six distributions for all three species groups (Vuong tests, $p < 0.001$; Table 2). In all other pair-wise comparisons, the distribution with the highest likelihood value was judged closer to the true model than the inferior model, although in some situations the difference between models was not significant.

Fig. 2 shows log-probability versus log-abundance plots for each distribution for simulated data using parameter values as estimated by maximum likelihood fitting to combined flock size data from all species (Fig. 2 column 1) as compared to the actual data of all species groups combined (Fig. 2 column 2). The figure demonstrates that the positive Poisson, positive geometric, logarithmic, and positive negative binomial distributions are unable to account for the large flocks sizes that are observed in the data while the zeta and Yule are capable of producing flock sizes that are much larger than observed in the data. Fig. 2 highlights the superior fit of the discretized lognormal distribution –

Table 3

Parameter estimates for the top five models to the flock size data for: all species combined, Common eiders, Long-tailed ducks, and scoters (listed in order by AICc). The values shown are the parameters for each distribution as described in Appendix B. The six right-most columns of the table give summary statistics of the observed flock size data for each species (bold) as well as summary statistics of simulations of flock size under each fitted distribution. The summaries for each distribution are the mean values based on 10,000 simulations using each species' parameter estimates and size of the sample data. The last column is the standard deviation of the maximum count over the 10,000 simulations. Note that the MLE parameters for the negative binomial and logarithmic distributions are such that the estimated mean of the distribution is the sample mean by definition.

	Parameter estimates		1st quartile	Median	Mean	3rd quartile	Max	SD(max)
All species			2	3	13.59	9	5000	
Discretized lognormal	$\mu = 1.093$	$\sigma = 1.478$	2.00	4.00	10.03	9.11	993.72	634.77
Logarithmic	$p = 0.982$		1.89	4.45	13.59	14.50	343.81	58.40
Positive negative binomial	$\mu = 0.438$	$k = 0.008$	1.96	4.63	13.54	14.57	338.26	59.22
Yule	$a = 0.610$		1.00	2.00	4.6E+06	7.88	3.9E+10	3.3E+12
Zeta	$a = 0.518$		2.00	4.00	2.0E+07	14.56	1.7E+11	9.6E+12
Common eiders			2	3	16.63	9	2000	
Discretized lognormal	$\mu = 0.866$	$\sigma = 1.680$	1.14	3.40	11.83	9.45	959.22	843.11
Yule	$a = 0.609$		1.00	2.03	3.6E+04	7.84	6.2E+07	1.7E+09
Zeta	$a = 0.521$		2.00	3.96	1.4E+08	14.37	2.4E+11	2.2E+13
Logarithmic	$p = 0.986$		1.97	5.05	16.63	17.34	347.07	75.37
Positive negative binomial	$\mu = 0.419$	$k = 0.006$	1.99	5.13	16.89	17.69	350.89	76.29
Long-tailed ducks			2	3	11.32	7	750	
Discretized lognormal	$\mu = 0.886$	$\sigma = 1.526$	1.03	3.01	9.13	8.16	649.26	459.21
Yule	$a = 0.652$		1.00	2.00	1.5E+04	6.84	4.1E+07	1.5E+09
Logarithmic	$p = 0.977$		1.16	4.00	11.33	12.33	231.47	47.87
Positive negative binomial	$\mu = 0.314$	$k = 0.008$	1.23	4.00	11.29	12.35	227.77	46.70
Zeta	$a = 0.548$		2.00	3.64	8.2E+05	12.56	2.2E+09	1.0E+11
Scoters			2	4	13.80	10	5000	
Discretized lognormal	$\mu = 1.286$	$\sigma = 1.369$	2.00	4.00	9.97	9.94	589.93	359.30
Logarithmic	$p = 0.982$		1.85	4.57	13.80	14.71	315.93	60.20
Positive negative binomial	$\mu = 0.919$	$k = 0.017$	1.98	4.90	14.04	15.15	313.52	61.90
Yule	$a = 0.586$		2.00	2.06	1.2E+05	8.48	4.9E+08	1.3E+10
Zeta	$a = 0.498$		2.00	4.00	9.0E+07	16.20	3.6E+11	2.4E+13

which best captures the range of variation observed in the right tail – to the sea duck data as compared to the other six distributions.

The parameter estimates for the top models were comparable among species groups with estimates generally being more similar between Common eiders and Long-tailed ducks as compared to scoters (Table 3). In the parameterization of the zeta and Yule distributions that we present (Appendix B), the mean is not finite for values of $a < 1$ [10,50], yet for all three species groups the maximum likelihood estimates for these parameters were less than one. Thus, in order to compare the output from the fit of each statistical distribution, we simulated count data for each species group that was the size of the sample data ($n_{\text{all}} = 8498$; $n_{\text{common eider}} = 1742$; $n_{\text{long-tailed ducks}} = 2709$; $n_{\text{scoters}} = 4047$) 10,000 times and report the mean values for the summary statistics (Table 3). These results demonstrate the relationship between sample moments and moments of MLE fitted distributions. Note that the mean of the fitted logarithmic and negative binomial distributions match the observed sample mean (as expected given that the sample mean is the maximum likelihood estimator of the negative binomial and logarithmic means), but result in too many moderately large groups (3rd quartile), too few very large groups (maximum), and an underestimation of the variance observed in the data. Thus, although the fitted negative binomial and logarithmic distributions describe the mean of the data well, they mischaracterize other aspects of the data distribution and underestimate uncertainty about the mean. On the other end of the spectrum, the Yule and zeta distributions have unrealistically heavy tails and overestimate the variance in the counts. For example, the average standard deviation of flock size for all species combined (as estimated from simulations) was 1.15E+09 for the zeta distribution as compared to 25.8 for the discretized lognormal and 23.6 for the negative binomial (and 91.1 in the observed data). Although the standard deviation of flock size is only slightly higher with the discretized lognormal as compared to the logarithmic and negative binomial

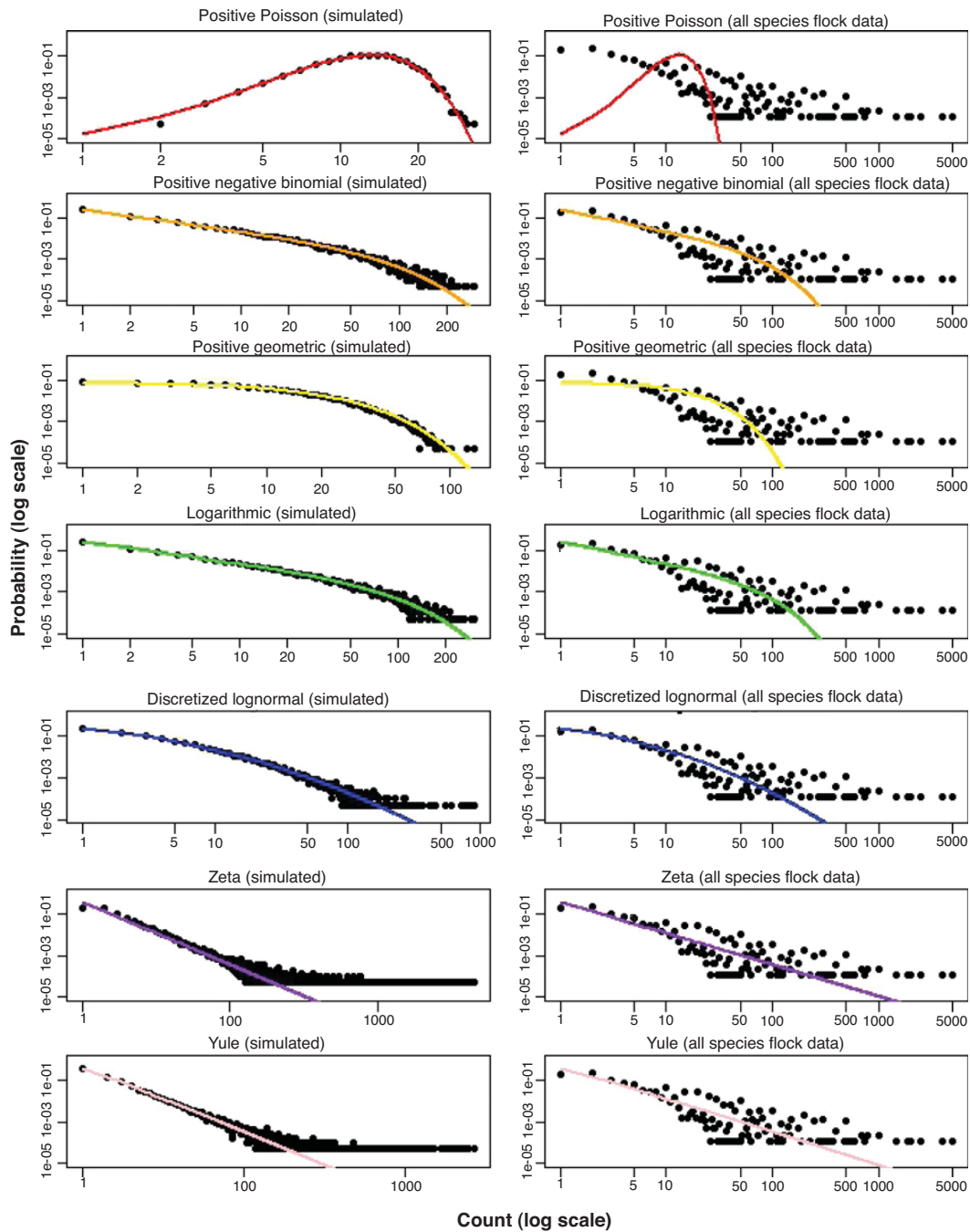


Fig. 2. Simulated (left column) and observed (right column) data for all species fitted using the seven distributions that we compared. Note the variable x-axes for the simulated data.

distributions, the latter two distributions are more likely to underestimate maximum flock size (last column, Table 3). The discretized lognormal distribution best matches the range of the observed data (Fig. 2, Table 3) but it also consistently underestimates the mean flock size, in part because it produces too few very large counts. Thus, while the discretized lognormal captures the variance and the upper tail probability of the data somewhat better than the other distributions (negative binomial and logarithmic underestimate upper tail probability and variance; zeta and Yule overestimate upper tail probability and variance), this comes at a cost to efficient estimation of the mean (negative bias of 20%–30% in our simulations). Given this result, Poisson mixture distributions may currently be preferable for abundance estimation, assuming reasonable variance corrections can be incorporated.

4. Discussion

We described a marked point process framework for modeling flock numbers and flock sizes to characterize sea duck distribution and abundance in the Atlantic. We employed model selection techniques to choose appropriate models for skewed and zero-inflated distributions of flock numbers and highly right-skewed distributions of flock sizes. Our process-oriented approach should be useful in modeling other highly aggregated, patchily distributed species. The distributions that best fit the “points”, i.e., the number of flocks per transect, (negative binomial and zero inflated negative binomial) and “marks”, i.e., the flock sizes, (discretized lognormal) were surprisingly consistent across sea duck species and did not vary among years.

Our results have important implications for estimating annual abundances of wintering sea ducks and for designing future surveys that will be able to generate information on population statuses and trends. Inappropriate choice of the distribution family in a modeling framework can lead not only to bias in parameter estimates, but to inaccurate assessments of uncertainty and statistical power. Appropriate characterization of uncertainty and estimation of statistical power are of particular importance in a management context because uncertainty will be propagated through decision-making processes and will affect our understanding of population dynamics, as well as the design and implementation of future monitoring programs. For example, national harvest regulations for many species of ducks are set annually by the US Fish and Wildlife Service using population estimates derived from aerial surveys of breeding areas (e.g., [46,48]); these regulatory decisions are informed by predictions from models of population dynamics that are also derived from survey estimates. Because the sea ducks considered here breed in remote areas that are not covered by current surveys, estimates from winter areas may provide our best means of monitoring responses to exploitation and environmental change, but only if estimates from winter surveys can correctly and precisely estimate abundance. Our results are also particularly relevant to applications that require proper modeling of the extreme values of abundance observed for many species and where surveying presents logistical challenges, thereby limiting the number of samples collected. This includes risk and impact assessments, as well as detection of high-use areas. As marine environments along the eastern United States are currently being considered for development of wind energy production [5], sufficient survey methods and accurate maps are critically needed to assess the potential impacts of the proposed development on sea ducks and seabirds.

The best-fitting distributions for flock size in our study (discretized lognormal, logarithmic, negative binomial, Yule, and zeta) differ from each other primarily in the shape of the upper tail. The probability mass of the zeta distribution declines log-linearly in the tail (that is, linearly on doubly logarithmic axes), and the Yule distribution nearly so, making them the heaviest tailed distributions in our candidate set. This is evident in the relatively common occurrence of very large counts in these distributions (column one in Fig. 2, Table 3). The probability mass of the upper tail of the discretized lognormal distribution declines in a log-quadratic fashion, whereas the logarithmic and negative binomial display an exponential decay in the upper tail. Thus, the heaviness of tails in these distributions is ranked as follows: zeta \approx Yule $>$ discretized lognormal $>$ logarithmic \approx negative binomial. That the discretized lognormal distribution was consistently selected for our three sea duck species groups suggests that the upper tails of flock size distributions for these species are not exponentially bounded (logarithmic and negative binomial), but not as extreme as would be predicted under power law-type distributions (e.g., zeta, Yule). This is fortunate for abundance estimation, because power law behavior implies that the variance (for $a < 2$) and mean (for $a < 1$) are not finite; that is, that sample moments would increase with the area and time spent sampling rather than providing estimates of meaningful characteristic properties of the abundance distribution.

The lognormal distribution has a long history in ecology (e.g., [38]) and a diversity of other fields [27] where it often arises as a plausible alternative to other heavy-tailed distributions like power laws (e.g., in birds; [1]). One classical generative process for a lognormal distribution is the multiplicative stochastic growth process first proposed by Gibrat [16], in which the size of an entity changes by successive multiplicative random effects; if the multiplicative random effects are independent and lognormally distributed, then the size distribution will be lognormal. The lognormal distribution arises even more generally as a direct consequence of the Central Limit Theorem for

products of random variables; any process that involves the product of a sufficiently large number of independent and identically distributed random variables having any distribution with finite mean and variance has a limiting lognormal distribution. Thus, a discretized lognormal distribution of counts could arise from a variety of plausible ecological mechanisms. However, the lognormal distribution is known to produce biased estimates of the mean and variance when it is “contaminated” with even small amounts of data from other distributions [32]. In our dataset of flock sizes, the discretized lognormal underestimated the sample mean for all three species (Table 3), which suggests that our data may not conform perfectly to a lognormal distribution. One possible reason for small deviations from lognormality might be nonstationarity in the underlying process. It may be possible to control for this problem by stratifying areas of high/low abundance or adding covariates that account for changes in group sizes, such that the conditional distribution is closer to lognormal. The lack-of-fit of the lognormal may also reflect the manner in which observers count birds in aerial surveys: singles and pairs have a higher probability of being undetected [37], whereas flocks with more birds are typically undercounted [35]. Further exploration of the counting process and the relationship of the observed counts to actual sea duck flock sizes might help explain the disparity between the observed and lognormal tails. The ultimate choice of which distribution is the most appropriate depends on the modeling purpose. In our case, the discretized lognormal was identified as the best fitting distribution overall, and therefore might be the best choice for simulation modeling that requires a compact representation of the whole distribution. Yet, given the sensitivity of moment estimators to slight deviations from the lognormal distribution [32], one might be justified in choosing a statistical distribution with a lower total log-likelihood that can provide more robust mean abundance estimates, such as the logarithmic or negative binomial distributions. Simulation studies could help to choose the optimal distribution for particular applications.

Bonabeau et al. [4] suggested that an exponentially decaying power law may be a useful distribution for dealing with heavy-tailed data that is bounded. To determine the appropriateness of the exponentially decaying zeta distribution compared to our top performing models, we additionally fit this distribution to flock size data for the three species groups. While the exponentially decaying zeta distribution had greater log-likelihood values (-5324.3 for Common eiders, -7854.3 for Long-tailed ducks, and -12713.0 for scoters) than either the zeta or Yule (suggesting a comparatively better fit; Table 2), it was still outperformed by the discretized lognormal ($p < 0.001$ in Vuong pair-wise comparison tests and lower AICc) for all three species groups, supporting the hypothesis that our data, while skewed, are less heavy-tailed than distributions in the power law family. Although the exponentially decaying power law may not produce a better fit to our data than the discretized lognormal, it may provide a useful alternative because of the above mentioned problems associated with estimating the moments of lognormal distributions when the lognormal is not a perfect fit. By no means did we present an exhaustive list of possible statistical distributions for modeling skewed count data. We suggest further exploration of the exponentially decaying zeta distribution, as well as other distributions as possible alternatives to the discretized lognormal, when abundance estimation is the objective.

It is important to note that selection among statistical distribution models that differ primarily in their tails is notoriously difficult with small sample sizes and noisy data [2,10]. We have used data from a very large survey, but many ecological datasets are substantially smaller and would not allow discrimination among the more similar of the models studied here [32]. This suggests a useful role for meta-analysis, synthetic analysis of large databases, and validation of mechanistic models of processes determining group size distributions, so that recommendations for appropriate choices of distributions can be made for selection of distributions on the basis of taxonomy, life history, environment, etc. The similarity in model fits among species, species groups, and years is encouraging, as it suggests that model power and estimator precision for individual species groups can be gained by borrowing information both over time and across species [48].

Many mechanistic models of group size formation and aggregation have been proposed to give rise to several of the distributions studied here. For example, Caraco [8], Niwa [33] and Ma et al. [29] have each demonstrated how differing rules related to the decision on when to join or leave groups can lead to negative binomial, decaying power law, and logarithmic distributions of group size, respectively. However, in our sea duck example, flock detection and flock size counts are likely the result not only of the biological processes associated with flocks coalescing, but also the specific fixed-width

sampling protocol used during the surveys (i.e., the observation process). In this case, the negative binomial distribution combined with the discretized lognormal produced the best fit to our marked point process for observed number of flocks and flocks sizes, but it is possible that other sampling approaches could yield different combinations. Counting large flocks on the ocean within a 200 m strip while in a fast moving airplane is a difficult task, but one that can be improved through training and revised protocols. Beauchamp [2] noted that rough conditions at sea could bias counts and possibly alter which statistical distribution fits best to observed flock sizes. Further exploration of how to minimize and account for the effects of the observation process, such as including covariates, detection functions, and upper limits imposed by the size of the observation unit, may lead to more accurate and precise counts and better estimates of uncertainty, allowing for improved understanding of the biological mechanisms that produce variation in sea duck flock sizes.

Statistical models of ecological count data can be far more complex than those presented here. It is common to include spatial, temporal, and habitat strata, environmental and biological covariates influencing ecological processes leading to the presence or absence of a species, and sampling covariates, which can affect the detection process of individuals during surveying. We intentionally focused our study on simple distributional models for avian count data, neglecting additional complexity that may in some cases improve model explanatory power. It is fundamental to first determine what form of the underlying statistical distribution is appropriate before real world complexities can be incorporated into models. Our marked point process approach matches the observational process (e.g., seeing a flock, then determining its size) and readily allows for inclusion of covariates for both flock detection and flock size estimation.

A parsimonious approach is recommended for a second reason: large scale monitoring programs often do not have the capacity to collect, maintain, and utilize extensive ancillary data sets, and long-term changes in distribution, abundance, or phenology may make models calibrated to fixed strata (e.g., the study area; areas of high density) inappropriate or inefficient at large scales. Thus, simple descriptions that generalize across species and years are extremely valuable, when possible. Our results suggest that the sea duck counts based on our survey methodology have similar statistical properties, and comparable models can be used over time and across species. These models will form the basis for continued exploration aimed at identifying the covariates affecting wintering sea duck populations, and providing decision makers with the best possible description of sea duck distributional patterns and trends.

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Appendix A

Parameters and probability mass functions for the four distributions that we compare using the data on the number of sea duck flocks per transect. In all cases, the support is $x \in \{0, 1, 2, 3, \dots\}$.

Specifications of all distributions are as in the VGAM R package [50].

Distribution	Parameters	Probability mass function	
		$P[X = 0]$	$P[X = x]$
Zero-inflated Poisson	$0 \leq \varphi \leq 1$ $\lambda > 0$	$\varphi + (1 - \varphi) e^{-\lambda}$	$(1 - \varphi) \frac{\lambda^x e^{-\lambda}}{x!}$
Zero-inflated geometric	$0 \leq \varphi \leq 1$ $0 < p \leq 1$	$\varphi + (1 - \varphi) p$	$(1 - \varphi) p (1 - p)^x$
Zero-inflated negative binomial	$0 \leq \varphi \leq 1$ $\mu > 0$ $k > 0$	$\varphi + (1 - \varphi) \left(\frac{k}{\mu + k}\right)^k$	$(1 - \varphi) \text{dnbinom}(x, \mu, k)$
Negative binomial	$\mu > 0$ $k > 0$	$\text{dnbinom} = \binom{x + k - 1}{x} \left(\frac{\mu}{\mu + k}\right)^x \left(\frac{k}{\mu + k}\right)^k$	

Appendix B

Parameters and probability mass functions for the seven distributions that we compare using the sea duck flock size data. In all cases, the support is $x \in \{1, 2, 3, \dots\}$. Specifications of all distributions are as in the VGAM R package [50] except for the discretized lognormal which is specified as in Clauset et al. [10].

Distribution	Parameters	Probability mass function
Positive Poisson	$\lambda > 0$	$\frac{\lambda^x e^{-\lambda}}{x!} \frac{1}{1 - e^{-\lambda}}$
Positive negative binomial	$\mu > 0$ $k > 0$	$\frac{\left(\frac{\Gamma(x + k)}{x! \Gamma(k)}\right) \left(\frac{\mu}{\mu + k}\right)^x \left(\frac{k}{\mu + k}\right)^k}{1 - \left(\frac{k}{\mu + k}\right)^k}$
Geometric	$0 < p \leq 1$	$p (1 - p)^{x-1}$
Logarithmic	$0 < p < 1$	$\frac{-1}{\ln(1 - p)} \frac{p^x}{x}$
Discretized lognormal	$-\infty < \mu < \infty$ $\sigma > 0$	$\frac{\exp\left(-\frac{(\ln(x - 0.5) - \mu)^2}{2\sigma^2}\right)}{(x - 0.5)\sqrt{2\pi\sigma^2}} - \frac{\exp\left(-\frac{(\ln(x + 0.5) - \mu)^2}{2\sigma^2}\right)}{(x + 0.5)\sqrt{2\pi\sigma^2}}$ $\frac{1}{\sqrt{\frac{2}{\pi\sigma^2}} \exp\left(-\frac{(\ln(0.5) - \mu)^2}{2\sigma^2}\right)}$
Zeta	$a > 0$	$\frac{1}{x^{a+1}} \bigg/ \sum_{n=1}^{\infty} \frac{1}{n^{a+1}}$
Yule	$a > 0$	$\frac{a \Gamma(x) \Gamma(a + 1)}{\Gamma(x + a + 1)}$

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